

A2 Mathematics Unit 4: Applied Mathematics B

General instructions for marking GCE Mathematics

1. The mark scheme should be applied precisely and no departure made from it. Marks should be awarded directly as indicated and no further subdivision made.
2. Marking Abbreviations
The following may be used in marking schemes or in the marking of scripts to indicate reasons for the marks awarded.
 - cao = correct answer only
 - MR = misread
 - PA = premature approximation
 - bod = benefit of doubt
 - oe = or equivalent
 - si = seen or implied
 - ISW = ignore subsequent working

F.T. = follow through (✓ indicates correct working following an error and ✗ indicates a further error has been made)

Anything given in brackets in the marking scheme is expected but, not required, to gain credit.
3. Premature Approximation
A candidate who approximates prematurely and then proceeds correctly to a final answer loses 1 mark as directed by the Principal Examiner.
4. Misreads
When the data of a question is misread in such a way as not to alter the aim or difficulty of a question, follow through the working and allot marks for the candidates' answers as on the scheme using the new data.
This is only applicable if a wrong value, is used consistently throughout a solution; if the correct value appears anywhere, the solution is not classed as MR (but may, of course, still earn other marks).
5. Marking codes
 - 'M' marks are awarded for any correct method applied to appropriate working, even though a numerical error may be involved. Once earned they cannot be lost.
 - 'm' marks are dependant method marks. They are only given if the relevant previous 'M' mark has been earned.
 - 'A' marks are given for a numerically correct stage, for a correct result or for an answer lying within a specified range. They are only given if the relevant M/m mark has been earned either explicitly or by inference from the correct answer.
 - 'B' marks are independent of method and are usually awarded for an accurate result or statement.
 - 'S' marks are awarded for strategy
 - 'E' marks are awarded for explanation
 - 'U' marks are awarded for units
 - 'P' marks are awarded for plotting points
 - 'C' marks are awarded for drawing curves

GCE AS and A LEVEL MATHEMATICS Sample Assessment Materials 60

Qu. No.	Solution	Mark	AO	Notes
2(a)(i)	$P(\text{J wins with 1}^{\text{st}} \text{ shot}) = P(\text{M misses}) \times P(\text{J hits})$ $= 0.75p$	M1 A1	AO1 AO1	
(ii)	<p>J wins with his second shot if the first three shots miss and then J hits the target with his second shot.</p> $P(\text{J wins with 2}^{\text{nd}} \text{ shot}) = 0.75 \times (1 - p) \times 0.75 \times p$	M1 A1	AO3 AO2	
(b)	$P(\text{J wins game}) = 0.75p + 0.75^2(1 - p)p + 0.75^3(1 - p)^2p + \dots$ <p>Attempting to sum an infinite geometric series</p> $= \frac{0.75p}{1 - 0.75(1 - p)}$ $= \frac{3p}{1 + 3p}$	M1 M1 A1	AO3 AO3 AO2	
(c)	<p>Mary is more likely to win if</p> $\frac{3p}{1 + 3p} < 0.5$ <p>leading to $p < \frac{1}{3}$</p>	M1 A1 [9]	AO3 AO1	
3(a)	<p>Continuous uniform distribution on [30,60] Mean = 45 Variance = 75</p>	B1 B1 B1	AO3 AO1 AO1	
(b)	$P(\pi R^2 > 100) = P\left(R > \sqrt{\frac{100}{\pi}}\right)$ $= P\left(L > 2\pi\sqrt{\frac{100}{\pi}}\right)$ $= P(L > 35.45)$ $= \frac{60 - 35.45}{30} = 0.818(3) \text{ or } \frac{491}{600}$	M1 A1 A1 A1 [7]	AO3 AO2 AO1 AO1	

GCE AS and A LEVEL MATHEMATICS Sample Assessment Materials 61

Qu. No.	Solution	Mark	AO	Notes
4(a)	Bell shaped	B1	AO2	Or Most values cluster in the middle of the range and the rest taper off symmetrically toward either extreme B0 for symmetrical only
(b)	$1 - P(6.12 < X < 8.12)$ $= 1 - 0.9949(0744)$ $= 0.0051$ (or 0.51%)	M1 A1	AO3 AO1	Or $P(X < 6.12) + P(X > 8.12)$ M1A0 For 0.9949(0744)
(c)(i)	The population of weights of 2p coins is normally distributed. Mean and median in the sample are very similar, suggesting a symmetric distribution.	B1 B1	AO2 AO2	B1B0 The weights of 2p coins are normally distributed. Population must be stated or implied.
(ii)	H_0 : The mean weight of all 2p coins in this batch = 7.12g H_1 : The mean weight of all 2p coins in this batch < 7.12g (one-sided) $p\text{-value} = P(\bar{x} < 6.89 \mid H_0)$ $= P\left(z < \frac{6.89 - 7.12}{\frac{0.357}{\sqrt{30}}}\right)$ $= P(z < -3.52(874))$ $= 0.00021$ (allow 0.00022) Since $p\text{-value} < 0.01$, Reject H_0 Very strong evidence to suggest the mean weight of the batch of 2p coins is less than 7.12(g)	B1 M1 A1 A1 A1 E1	AO3 AO1 AO1 AO2 AO3	Or $H_0: \mu = 7.12g$ B0 for H_0 : Mean = 7.12g Population must be stated or implied, ie. the batch of 2p coins FT two-sided test $p\text{-value} = 2 \times 0.00021 = 0.00042$
	Alternative Solution: $TS = \frac{6.89 - 7.12}{\frac{0.357}{\sqrt{30}}}$ $= -3.52(874)$ $CV = -2.32(63)$ Since $TS < CV$ Reject H_0 Very strong evidence to suggest the mean weight of the batch of 2p coins is less than 7.12(g)	(M1) (A1) (A1) (A1)	(AO1) (AO1) (AO1) (AO2)	FT Two-sided test $CVs = \pm 2.576$ Since $TS < -2.576$
		(E1)	(AO3)	
		[11]		

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Qu. No.	Solution	Mark	AO	Notes
5(a)	$H_0: \rho = 0$ $H_1: \rho \neq 0$ two-sided	B1	AO3	$H_0: \rho = 0$ $H_1: \rho > 0$ one-sided Population stated or implied
	TS = 0.895	B1	AO1	TS = 0.895
	CV = ± 0.4821	B1	AO1	CV = ± 0.412
	Since TS > 0.4821, Reject H_0 Strong evidence to suggest the correlation coefficient is greater than zero	B1	AO2	Since TS > 0.412, Reject H_0
		E1	AO3	Strong evidence to suggest the correlation coefficient is greater than zero
(b)	P-value for correlation between Value for money and Cost per night is > 0.05	E1	AO2	
	Cost per night does not seem to be correlated to Value for money.	E1	AO2	
		[7]		

SECTION B – Differential Equations and Mechanics

Question Number	Solution	Mark	AO	Notes
6. (a)	$\mathbf{a} = \mathbf{F}/m = \frac{1}{4}(4\mathbf{i} - 12\mathbf{j})$ $\mathbf{a} = \mathbf{i} - 3\mathbf{j}$ <p>Use $\mathbf{v} = \mathbf{u} + \mathbf{a}t$, $\mathbf{u} = -\mathbf{i} + 4\mathbf{j}$, $\mathbf{a} = \mathbf{i} - 3\mathbf{j}$</p> $\mathbf{v} = (-\mathbf{i} + 4\mathbf{j}) + 5(\mathbf{i} - 3\mathbf{j})$ $\mathbf{v} = 4\mathbf{i} - 11\mathbf{j}$	M1	AO3	
(b)	$\mathbf{s} = \mathbf{u}t + \frac{1}{2}\mathbf{a}t^2 + 7\mathbf{i} - 26\mathbf{j}$ $\mathbf{s} = 2(-\mathbf{i} + 4\mathbf{j}) + \frac{1}{2} \times 4 \times (\mathbf{i} - 3\mathbf{j})$ $+ (7\mathbf{i} - 26\mathbf{j})$ $\mathbf{s} = 7\mathbf{i} - 24\mathbf{j}$ $ \mathbf{s} = \sqrt{7^2 + 24^2}$ $ \mathbf{s} = 25$	M1 m1 A1 m1 A1 [8]	AO2 AO2 AO1 AO1 AO1 AO1	position vector relative to initial position vector. adding initial position vector.
7. (a)	<p>Attempt to resolve in 2 directions</p> $T_1 \cos 23^\circ = T_2 \cos 40^\circ$ $T_1 \sin 23^\circ + T_2 \sin 40^\circ = 160$ <p>Attempt to solve simultaneously</p> $T_1 = 137.56(028\dots) \text{ (N)}$ $T_2 = 165.29(707\dots) \text{ (N)}$	M1 A1 A1 m1 A1 A1 [8]	AO3 AO2 AO2 AO1 AO1 AO1	dimensionally correct equation, no omitted or extra forces correct equation correct equation any valid method
(b)	<p>Object modelled as particle Cable modelled as light strings</p>	B1 B1 [8]	AO3 AO3	

GCE AS and A LEVEL MATHEMATICS Sample Assessment Materials 65

Question Number	Solution	Mark	AO	Notes	
10.	(a)	$x = (V\cos\theta)t$	B1	AO1	
		$y = (V\sin\theta)t - \frac{1}{2}gt^2$	B1	AO1	
	(b)	$y = 0$ for time of flight	M1	AO2	
		$t = \frac{2V\sin\theta}{g}$			
		Range $R = V\cos\theta \cdot \frac{2V\sin\theta}{g}$	m1	AO2	
		$R = \frac{V^2\sin 2\theta}{g}$	A1	AO2	
	(c) (i)	At maximum range, $\sin 2\theta = 1$	M1	AO3	oe
		$\theta = 45^\circ$			
		$\frac{V^2}{g} = 392$			
		$V = 62.0 \text{ (ms}^{-1}\text{)}$	A1	AO1	cao
(ii)	$t = \frac{2 \times 62.0 \times \sin 45}{g}$				
	$t = 8.95 \text{ (s)}$	A1	AO1	cao	
(iii)	Max height when $t = 4.47 \text{ s}$,	m1	AO2		
	$y_{\max} = 62.5 \times \sin 45^\circ \times 4.47 - \frac{1}{2} \times 9.8 \times 4.47^2$				
	$y_{\max} = 98.1 \text{ (m)}$	A1	AO1	cao	
		[10]			